

PQ + φ + A

Q1

A racing car starts from rest and accelerates uniformly in a straight line at 12 m s^{-2} for 5 s. Calculate the final velocity of the car.

$$u = 0 \text{ m s}^{-1}$$

$$a = 12 \text{ m s}^{-2}$$

$$t = 5 \text{ s}$$

$$v = ?$$

$$v = u + at$$

$$v = u + at$$

$$v = 0 + (12 \times 5)$$

$$v = 0 + 60$$

$$v = 60 \text{ m s}^{-1} \text{ in direction of acceleration}$$

Q2

A speedboat travels 400 m in a straight line when it accelerates uniformly from 2.5 m s^{-1} in 10 s. Calculate the acceleration of the speedboat.

$$s = 400 \text{ m}$$

$$u = 2.5 \text{ m s}^{-1}$$

$$t = 10 \text{ s}$$

$$a = ?$$

$$s = ut + \frac{1}{2}at^2$$

~~s =~~

$$400 = (2.5 \times 10) + (0.5 \times a \times 10^2)$$

$$400 = 25 + 5a$$

$$5a = 400 - 25 = 375$$

$$a = \frac{375}{5} = 7.5 \text{ m s}^{-2} \text{ in the direction of original velocity}$$

Q3

A rocket is travelling through outer space with uniform velocity. It then accelerates at 2.5 m s^{-2} in a straight line in the original direction, reaching 100 m s^{-1} after travelling 1875 m . Calculate the rocket's initial velocity?

$$a = 2.5 \text{ m s}^{-2}$$

$$V = 100 \text{ m s}^{-1}$$

$$s = 1875 \text{ m}$$

$$u = ?$$

$$V^2 = u^2 + 2as$$

$$100^2 = u^2 + (2 \times 2.5 \times 1875)$$

$$10000 = u^2 + 9375$$

$$u^2 = 10000 - 9375 = 625$$

$$u = 25 \text{ m s}^{-1} \text{ in direction of acceleration}$$

Q4

A car, travelling in a straight line, decelerates uniformly at 2 m s^{-2} from 25 m s^{-1} for 3 s. Calculate the car's velocity after the 3 s.

$$a = -2 \text{ m s}^{-2}$$

$$u = 25 \text{ m s}^{-1}$$

$$t = 3 \text{ s}$$

$$v = ?$$

$$v = u + at$$

$$v = u + at$$

$$v = 25 + (-2 \times 3)$$

$$v = 25 + (-6)$$

$$v = \underline{19 \text{ m s}^{-1}} \text{ (in direction of original velocity)}$$

Q5

A greyhound is running at 6 m s^{-1} . It decelerates uniformly in a straight line at 0.5 m s^{-2} for 3 s. Calculate the displacement of the greyhound while it was decelerating.

$$u = 6 \text{ m s}^{-1}$$

$$a = -0.5 \text{ m s}^{-2}$$

$$t = 3 \text{ s}$$

$$s = ?$$

$$s = ut + \frac{1}{2}at^2$$

$$s = (6 \times 3) + (0.5 \times -0.5 \times 3^2)$$

$$s = 18 + (-2.25)$$

$$s = \underline{15.75 \text{ m}} \text{ (in direction of original velocity)}$$

$$s = ut + \frac{1}{2}at^2$$

Q6

A curling stone leaves a player's hand at 5 m s^{-1} and decelerates uniformly at 0.75 m s^{-2} in a straight line for 16.5 m until it strikes another stationary stone. Calculate the velocity of the decelerating curling stone at the instant it strikes the stationary one.

$$u = 5 \text{ m s}^{-1}$$

$$a = -0.75 \text{ m s}^{-2}$$

$$s = 16.5 \text{ m}$$

$$v = ?$$

$$v^2 = u^2 + 2as$$

$$v^2 = 5^2 + (2 \times -0.75 \times 16.5)$$

$$v^2 = 25 + (-24.75)$$

$$v^2 = 0.25$$

$$v = \sqrt{0.25} = \underline{0.5 \text{ m s}^{-1}} \text{ (in direction of original velocity)}$$

$$v^2 = u^2 + 2as$$

Q7

A firework rocket is launched vertically upwards from the ground at 49 m s^{-1} .

(a) What will be the velocity of the rocket at its maximum height?

(b) Calculate:

(i) the time taken for the rocket to reach its maximum height;

(ii) the maximum height.

$$u = 49 \text{ m s}^{-1}$$

$$a = -9.8 \text{ m s}^{-2}$$

$$t = ?$$

$$s = ?$$

$$\begin{array}{l} \text{(a)} \quad At \\ \text{maximum} \\ \text{height,} \\ v = 0 \text{ m s}^{-1} \end{array}$$

$$\text{(b)(i)} \quad v = u + at$$

$$0 = 49 + (-9.8 \times t)$$

$$0 = 49 - 9.8t$$

$$9.8t = 49$$

$$t = 49/9.8 = \underline{5 \text{ s.}}$$

$$\text{(ii)} \quad s = ut + \frac{1}{2}at^2$$

$$s = (49 \times 5) + (0.5 \times -9.8 \times 5^2)$$

$$s = 245 + (-122.5)$$

$$s = \underline{122.5 \text{ m}}$$

(i.e., 122.5 m upwards,
so height = 122.5 m)

$$v^2 = u^2 + 2as$$

$$0^2 = 49^2 + (2 \times -9.8 \times s)$$

$$0 = 2401 + (-19.6s)$$

$$19.6s = 2401$$

$$s = 2401/19.6 = \underline{122.5 \text{ m}}$$

(i.e., 122.5 m upwards,
so height = 122.5 m)

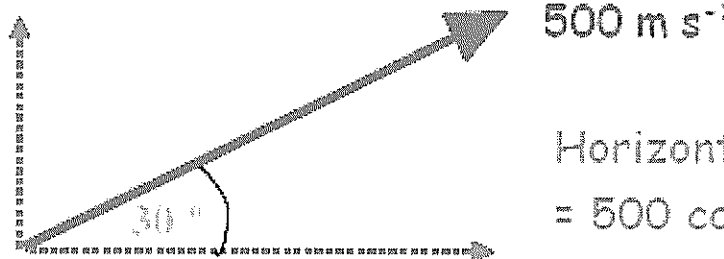
Q8

A long-range artillery shell is fired from level ground with a velocity of 500 m s^{-1} at an angle of 30° to the horizontal. Determine:

- the greatest height the shell reaches;
- the time taken to reach that height;
- the total time the shell is in the air;
- the horizontal distance the shell travels (i.e., its range).

First, resolve the velocity into its horizontal and vertical components:

$$\begin{aligned}\text{Vertical component of velocity} \\ &= 500 \sin 30^\circ \\ &= 500 \times 0.5 \\ &= 250 \text{ m s}^{-1}.\end{aligned}$$



$$\begin{aligned}\text{Horizontal component of velocity} \\ &= 500 \cos 30^\circ \\ &= 500 \times 0.866 \\ &= 433 \text{ m s}^{-1}.\end{aligned}$$

Q8 continued

(a)



v at highest point = 0

$$v^2 = u^2 + 2as$$

gravitational acceleration = -9.8 m s^{-2}

$$0^2 = 250^2 + (2 \times -9.8 \times s)$$

$$0 = 62\,500 - 19.6s$$

$$19.6s = 62\,500$$

$$s = 62\,500/19.6 = \underline{\underline{3\,189 \text{ m}}} \text{ (to nearest metre).}$$

Q8 continued

$$(b) v = u + at$$


$$0 = 250 + (-9.8 \times t)$$

$$0 = 250 - 9.8 t$$

$$9.8 t = 250$$

$$t = 250/9.8 = \underline{25.5 \text{ s}}$$

$$(c) \text{ Total time shell is in air} = 2 \times 25.5 \text{ s} = \underline{51 \text{ s}}$$


$$(d) s_h = v_h t$$

$$= 433 \times 51$$

$$= \underline{22\,083 \text{ m right}}$$